

Problem 1: Nbits

How many different integers between A and B (including A and B) have exactly N bits of 1 in the two's complement representation? That's the question to be answered in this problem.

Example

The problem is pretty clear. For example, suppose A is 5, B is 14, and N is 2. If we look at the two's complement binary representation of the integers between 5 and 14 and identify those with exactly 2 one bits, we find that there are five such numbers (identified by the left-pointing arrows)¹:

| | | | |
|---|-----------|----|-----------|
| 5 | 0 1 0 1 ← | 10 | 1 0 1 0 ← |
| 6 | 0 1 1 0 ← | 11 | 1 0 1 1 |
| 7 | 0 1 1 1 | 12 | 1 1 0 0 ← |
| 8 | 1 0 0 0 | 13 | 1 1 0 1 |
| 9 | 1 0 0 1 ← | 14 | 1 1 1 0 |

So the answer for this case would be 5.

Input

There will be multiple input cases to consider. For each case there will be a single input line containing A, B, and N. The input for the last case will be followed by a line containing three zeroes. A and B will each be in the range -2147483648 to +2147483647, and N will be in the range 1 to 32.

Output

For each input case, display the case number (1, 2, ...) and the appropriate number. Display a blank line after the output for each case. The sample input and output illustrate the appropriate formats.

| Sample Input | Output for the Sample Input |
|--------------|-----------------------------|
| 5 14 2 | Case 1: 5 numbers |
| 5 14 3 | Case 2: 4 numbers |
| -1 1 1 | Case 3: 1 numbers |
| 0 0 0 | |

¹ All the high-order bits in these numbers are 0; they are not shown for clarity.